



TED (15) – 1002

Reg. No.

(REVISION – 2015)

Signature

DIPLOMA EXAMINATION IN ENGINEERING/TECHNOLOGY/
MANAGEMENT/COMMERCIAL PRACTICE — OCTOBER, 2017

ENGINEERING MATHEMATICS – I

[Time : 3 hours

(Maximum marks : 100)

PART — A

(Maximum marks : 10)

Marks

I Answer all questions. Each question carries 2 marks.

1. Prove that $(1 + \cos A)(1 - \cos A) = \sin^2 A$
2. Find the value of $3\sin 15^\circ - 4\sin^3 15^\circ$
3. Find $\frac{dy}{dx}$ if $y = x^3 \tan x$.
4. Find the rate of change of volume V with respect to the side of a cube.
5. Find the area of triangle ABC given $B = 3\text{cm}$, $C = 2\text{cm}$ and $A = 30^\circ$

(5×2 = 10)

PART — B

(Maximum marks : 30)

II Answer any five of the following questions. Each question carries 6 marks.

1. Prove that $\left(\frac{\tan\theta + \sec\theta - 1}{\tan\theta - \sec\theta + 1}\right) = \frac{1 + \sin\theta}{\cos\theta}$
2. If $\tan A = \frac{m}{m+1}$, $\tan B = \frac{1}{2m+1}$ A and B are acute angles.
Prove that $A + B = 45^\circ$
3. Prove that $\sin 20^\circ \cdot \sin 40^\circ \cdot \sin 80^\circ = \frac{\sqrt{3}}{8}$
4. Prove that $R(a^2 + b^2 + c^2) = abc(\cot A + \cot B + \cot C)$ where R is radius of circumcircle.
5. Differentiate x^n by method of first principles.
6. A particle moves such that the displacement from a fixed point 'o' is always given by $S = 5\cos(nt) + 4\sin(nt)$ where n is a constant. Prove that the acceleration varies as its displacement S at the instant.
7. Find the equation to the tangent and normal to the curve $y = 3x^2 + x - 2$ at (1,2).

(5×6 = 30)



PART — C

(Maximum marks : 60)

(Answer *one* full question from each unit. Each full question carries 15 marks.)

UNIT — I

- III (a) Prove that $\left(\frac{1 + \sin A}{\cos A}\right) = \left(\frac{\cos A}{1 - \sin A}\right)$ 5
- (b) Prove that $\frac{\cos(90 + A) \sec(360 + A) \tan(180 - A)}{\sec(A - 720) \sin(540 + A) \cot(A - 90)} = 1$ 5
- (c) If $\sin A = \frac{-4}{5}$ and A lies in third quadrant, find all other trigonometric functions. 5

OR

- IV (a) If $\cos A = 3/5$, $\tan B = 5/12$, A and B are acute angles, find the values of $\sin(A + B)$ and $\cos(A - B)$. 6
- (b) Prove that $\frac{\tan 45 - \tan 30}{1 + \tan 45 \tan 30} = 2 - \sqrt{3}$ 4
- (c) Express $5 \sin x - 12 \cos x$ in the form $R \sin(x - \infty)$ 5

UNIT — II

- V (a) Prove that $\sin 33 + \cos 63 = \cos 3$ 5
- (b) Show that $(a-b) \cos \frac{C}{2} = c \sin \frac{A-B}{2}$ 5
- (c) Solve triangle ABC, given $a = 2\text{cm}$ $b = 3\text{cm}$ $c = 4\text{cm}$ 5

OR

- VI (a) Prove that $\cos \frac{\pi}{8} + \cos \frac{3\pi}{8} + \cos \frac{5\pi}{8} + \cos \frac{7\pi}{8} = 0$ 5
- (b) Prove that $2 [b \cos A + c \cos B + a \cos C] = a^2 + b^2 + c^2$ 5
- (c) Two angles of a triangular plot of land are $53^\circ 17'$ and $67^\circ 9'$ and the side between them is measured to be 150m. How many metres of fencing is required to fence the plot ? 5

UNIT — III

- VII (a) Evaluate $\lim_{x \rightarrow 0} \frac{\sqrt{1+x} - 1}{x}$ 4
- (b) Find $\frac{dy}{dx}$, if (i) $y = \frac{\cot 11x}{(x^3 - 1)^2}$ (ii) $(x^2 + 1)^{10} \sec^5 x$ (3+3)
- (c) If $x = a(\theta + \sin \theta)$ $y = a(1 - \cos \theta)$ find $\frac{dy}{dx}$ 5

OR



- | | Marks |
|--|-------|
| VIII (a) Find the derivative of $\cot x$ using quotient rule. | 5 |
| (b) If $y = \sin^{-1} x$ prove that $(1-x^2) \frac{d^2y}{dx^2} - x \frac{dy}{dx} = 0$ | 5 |
| (c) If x and y are connected by the relation $ax^2 + 2hxy + by^2 = 0$ find $\frac{dy}{dx}$. | 5 |

UNIT — IV

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| IX (a) Show that all the points on the curve $x^3 + y^3 = 3axy$ at which the tangents are parallel to the x -axis lie on the curve, $ay = x^2$. | 5 |
| (b) A spherical balloon is inflated by pumping 25cc of gas per second. Find the rate at which the radius of the balloon is increasing when the radius is 15 cm. | 5 |
| (c) The deflection of a beam is given by $y = 4x^3 + 9x^2 - 12x + 2$. Find the maximum deflection. | 5 |

OR

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| X (a) Prove that a rectangle of fixed perimeter has its maximum area when it becomes a square. | 5 |
| (b) A circular patch of oil spreads out on water, the area growing at the rate of 6 sq.cm per minute. How fast is the radius increasing when the radius is 2cms.? | 5 |
| (c) The distance travelled by a moving body is given by $S = 2t^3 - 9t^2 + 12t + 6$. Find the time when the acceleration is zero. | 5 |
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